

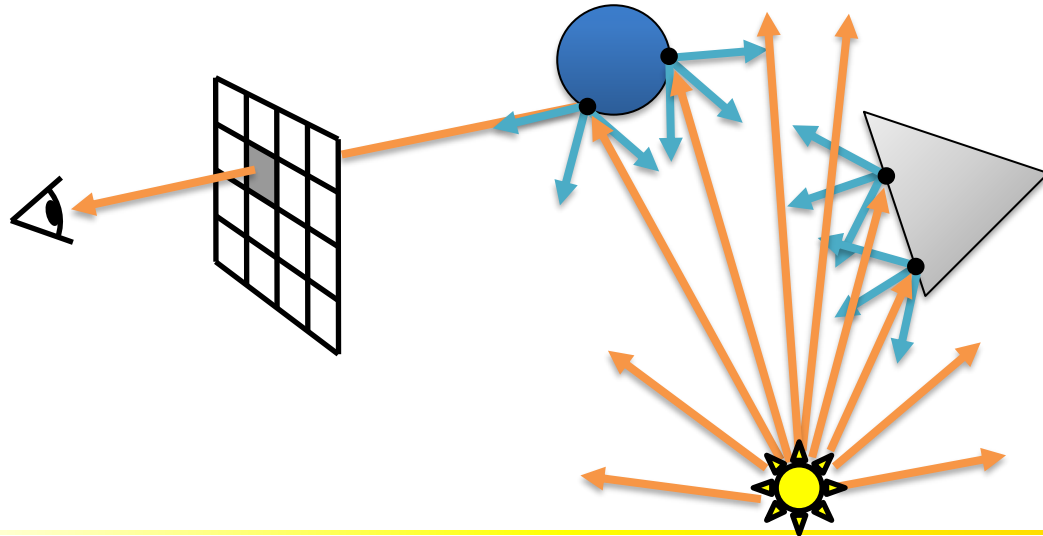
# Ray Tracing

Prof. Dr. Markus Gross



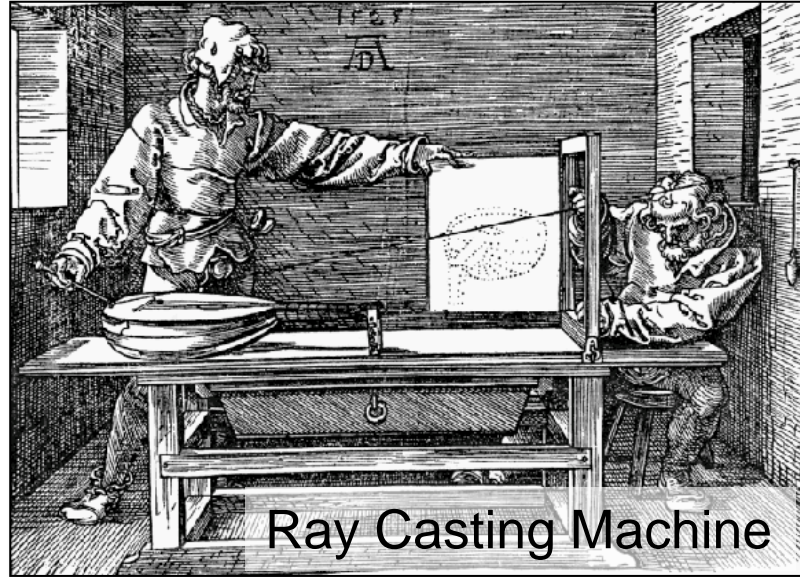
# Ray Tracing

- Send rays into the scene to determine the color of a pixel



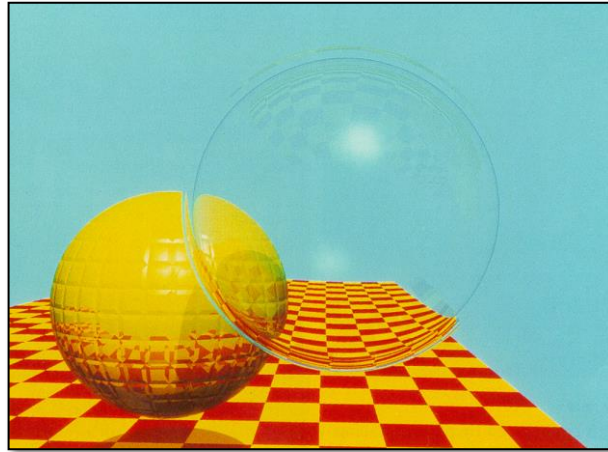
# Ray Tracing

- Albrecht Dürer (1525)



# Ray Tracing

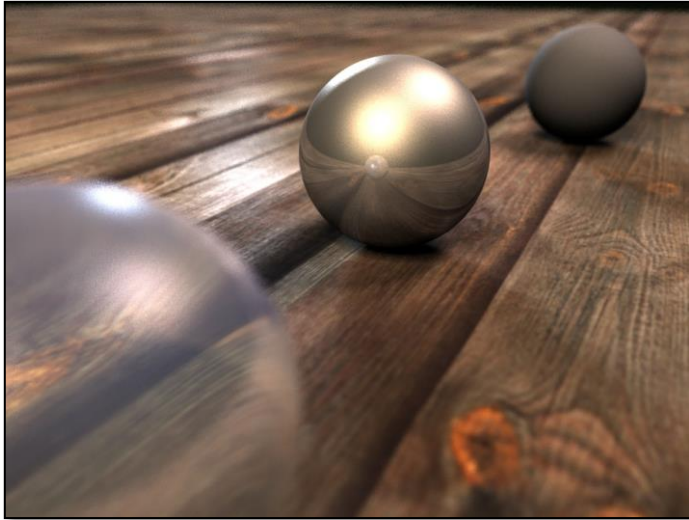
- Whitted (1979)



Recursive ray tracing (reflection & refraction)

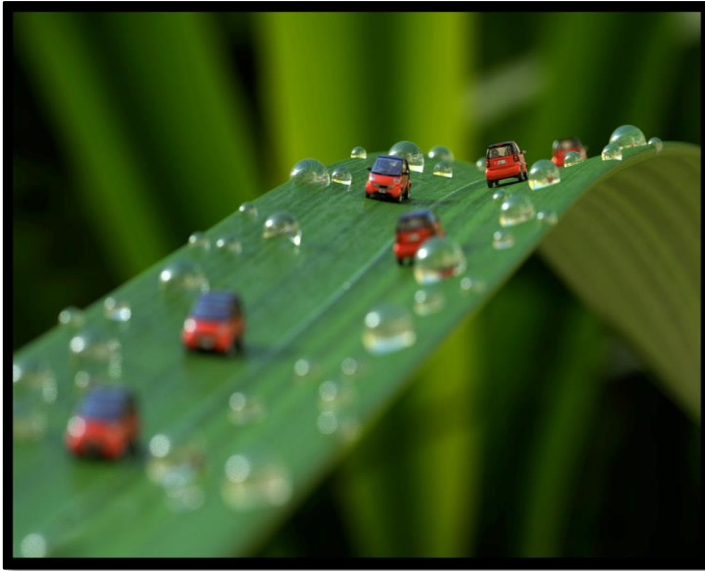
# Ray Tracing

- Today – high-quality renderings



# Ray Tracing

- Ray-traced images



# Ray Tracing

- Ray-traced images



# Ray Tracing

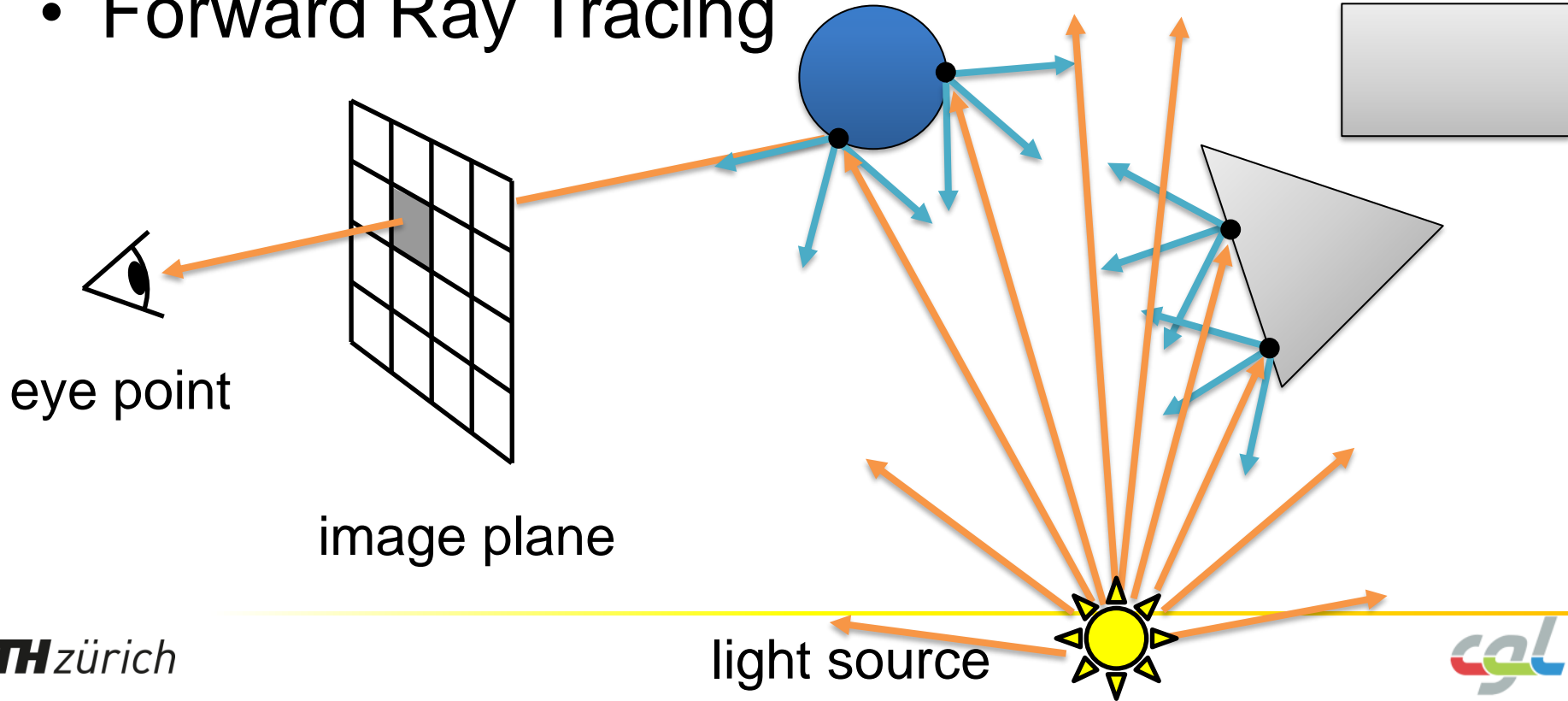
- Ray-traced images





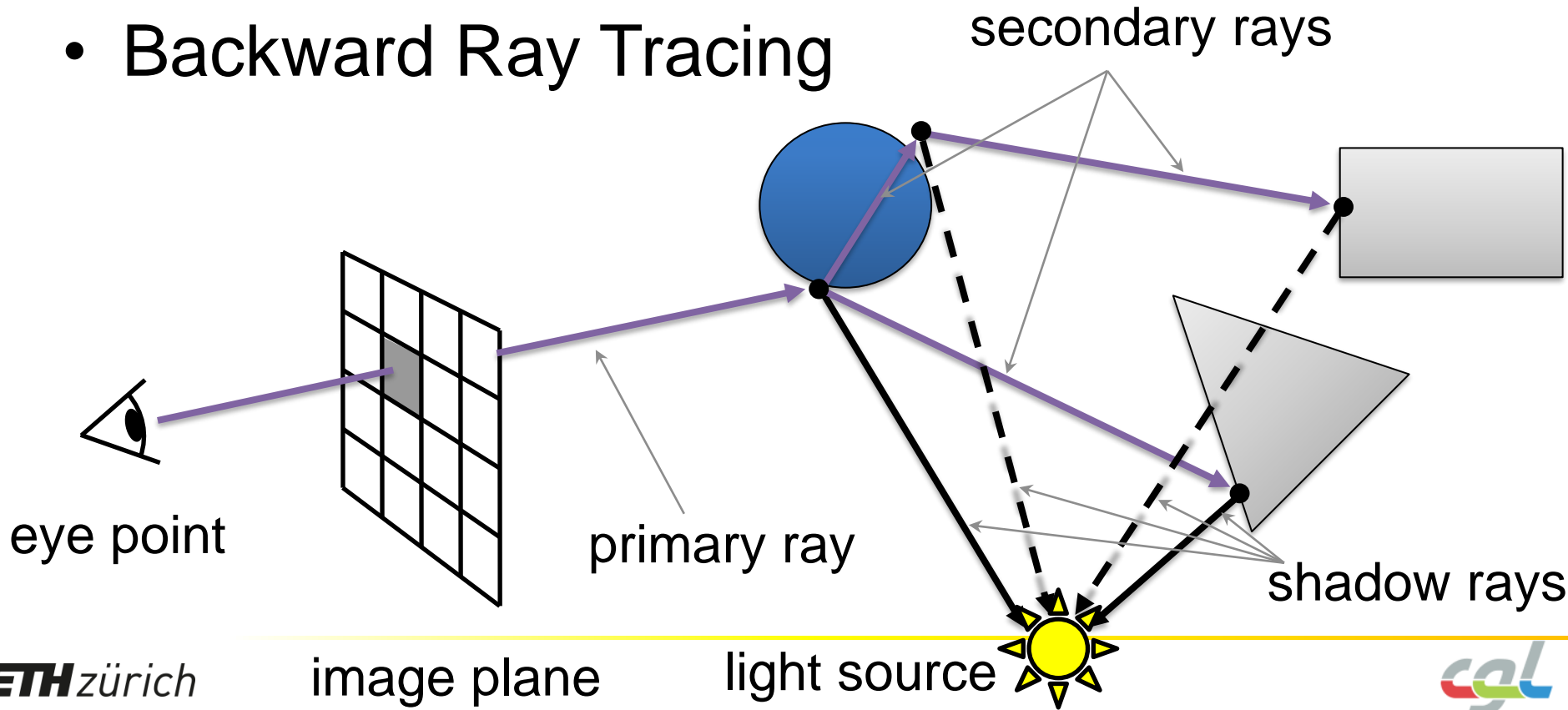
# Ray Tracing

- Forward Ray Tracing



# Ray Tracing

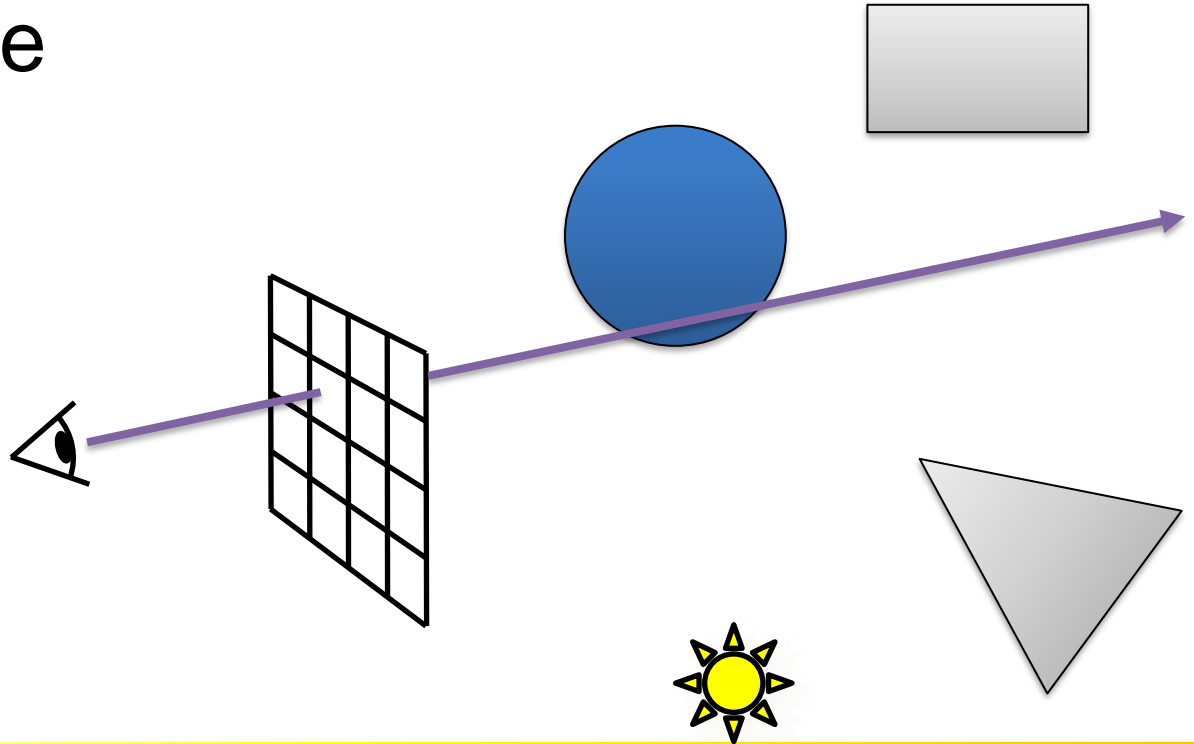
- Backward Ray Tracing



# Ray Tracing

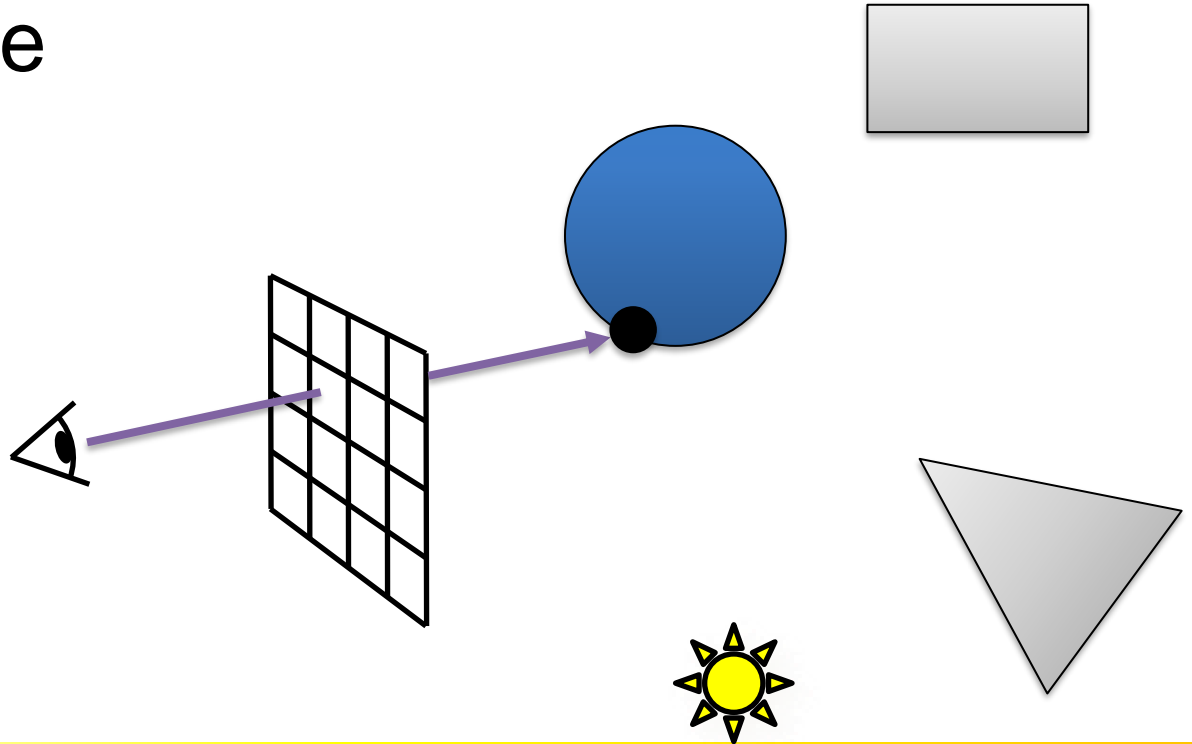
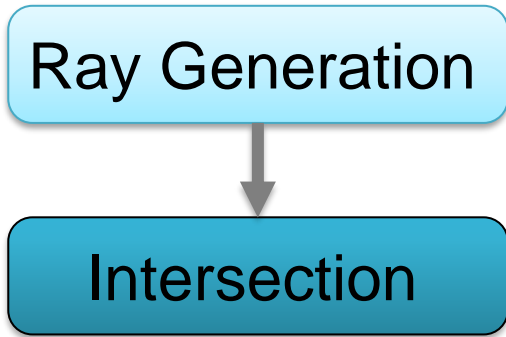
- Basic pipeline

Ray Generation



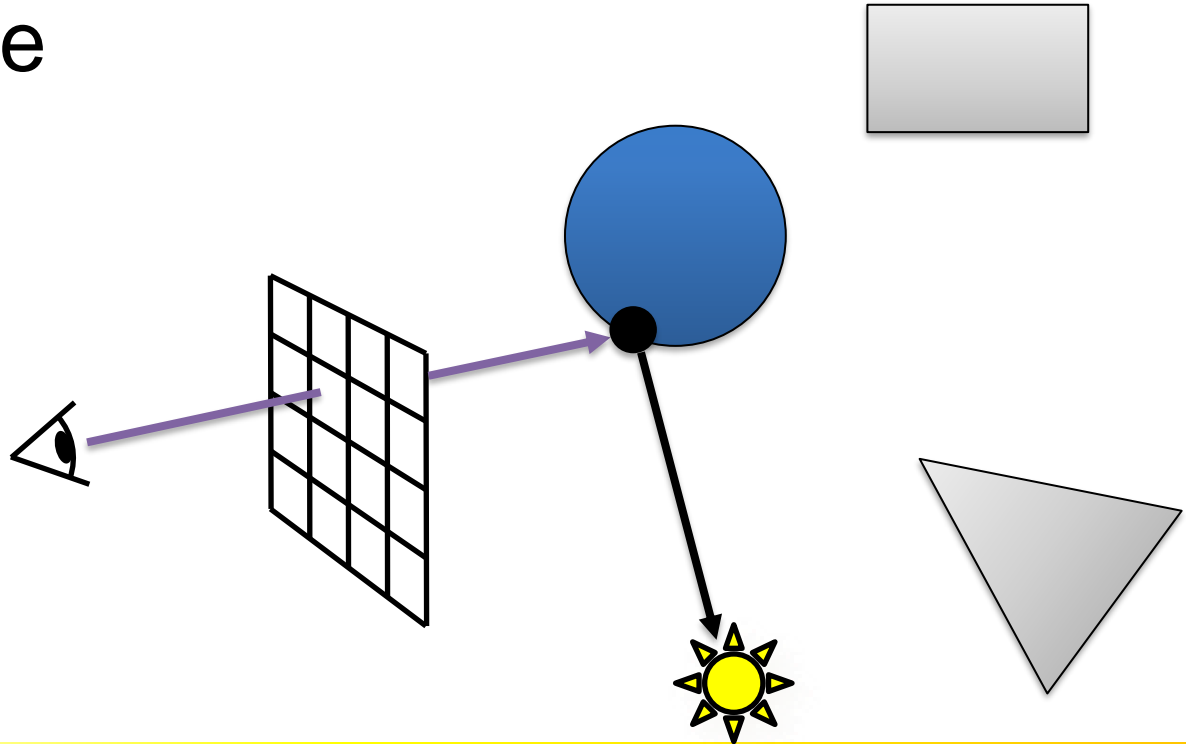
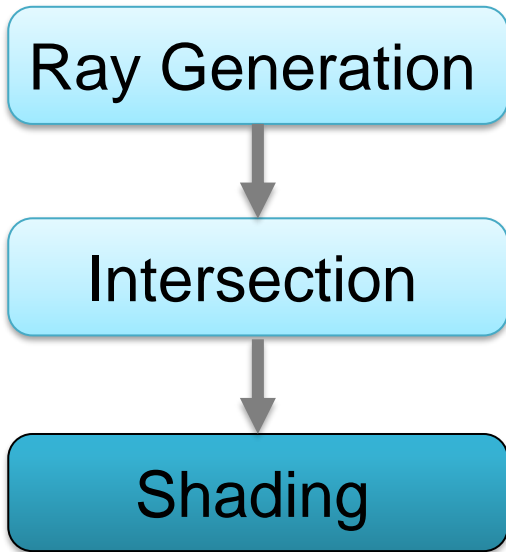
# Ray Tracing

- Basic pipeline



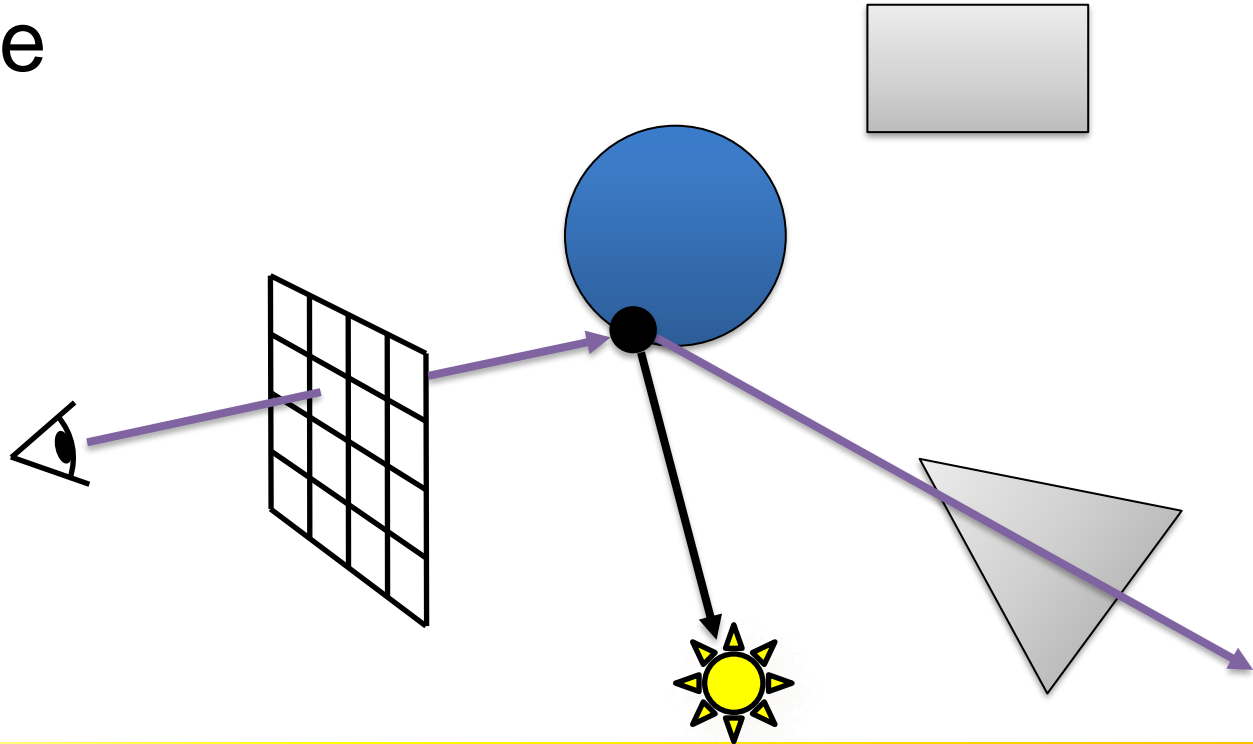
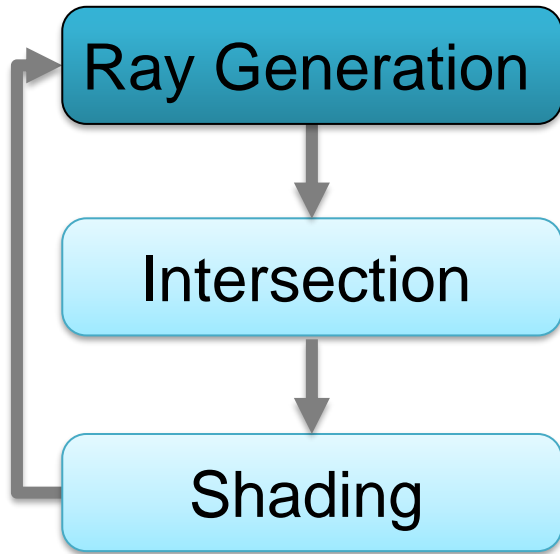
# Ray Tracing

- Basic pipeline



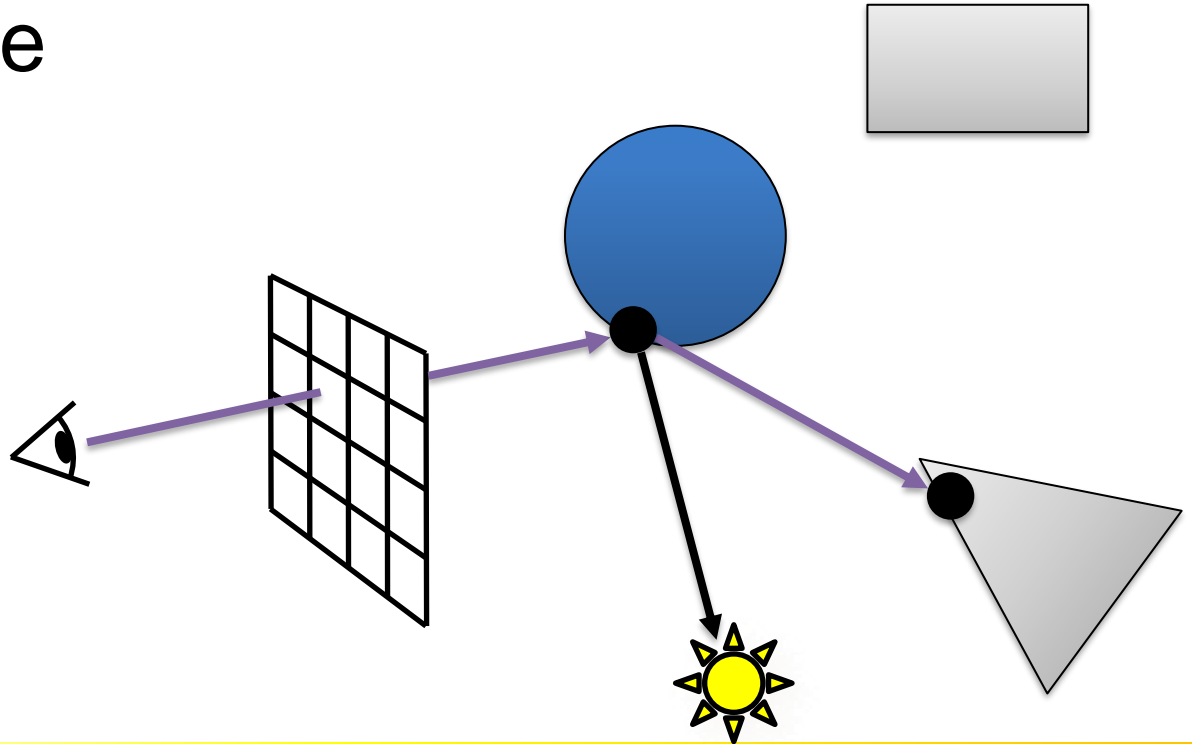
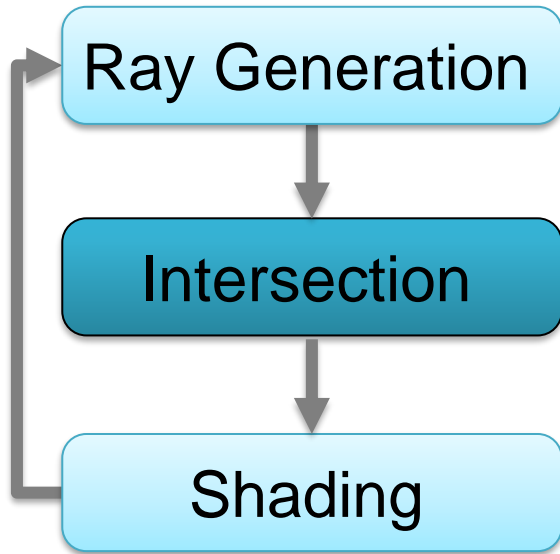
# Ray Tracing

- Basic pipeline



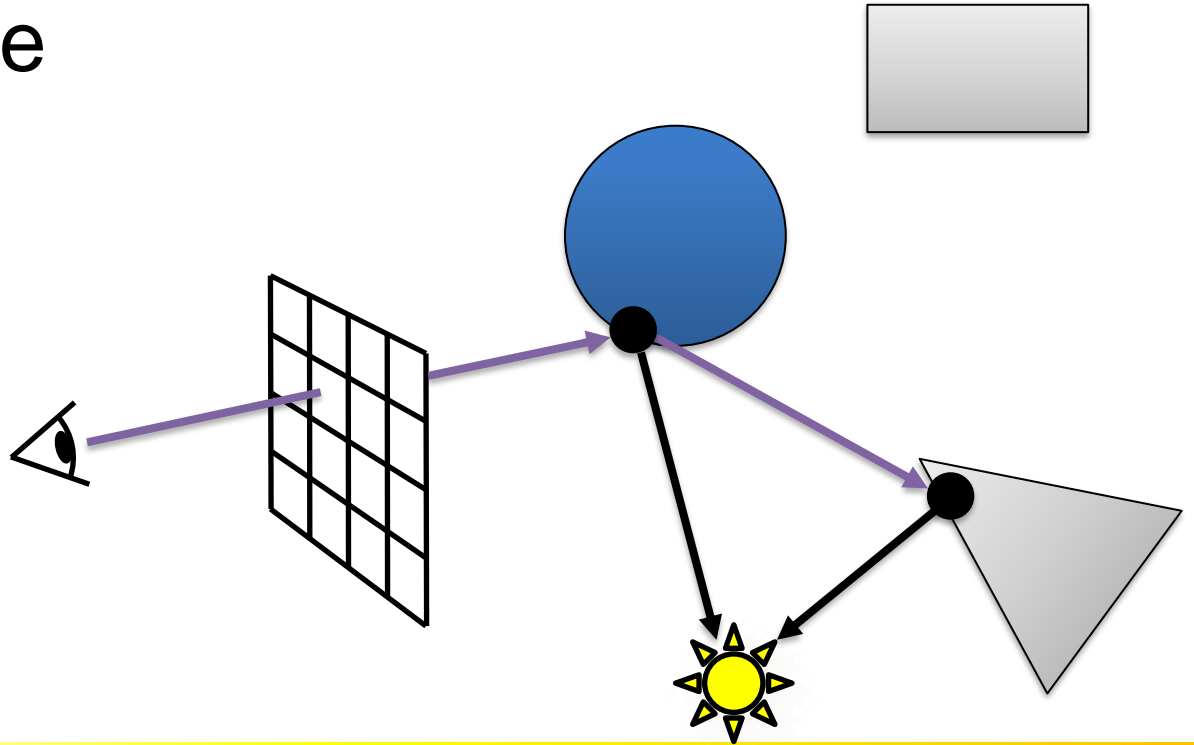
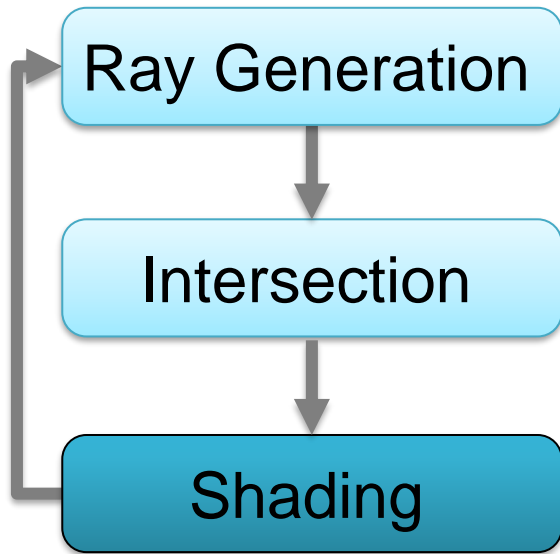
# Ray Tracing

- Basic pipeline



# Ray Tracing

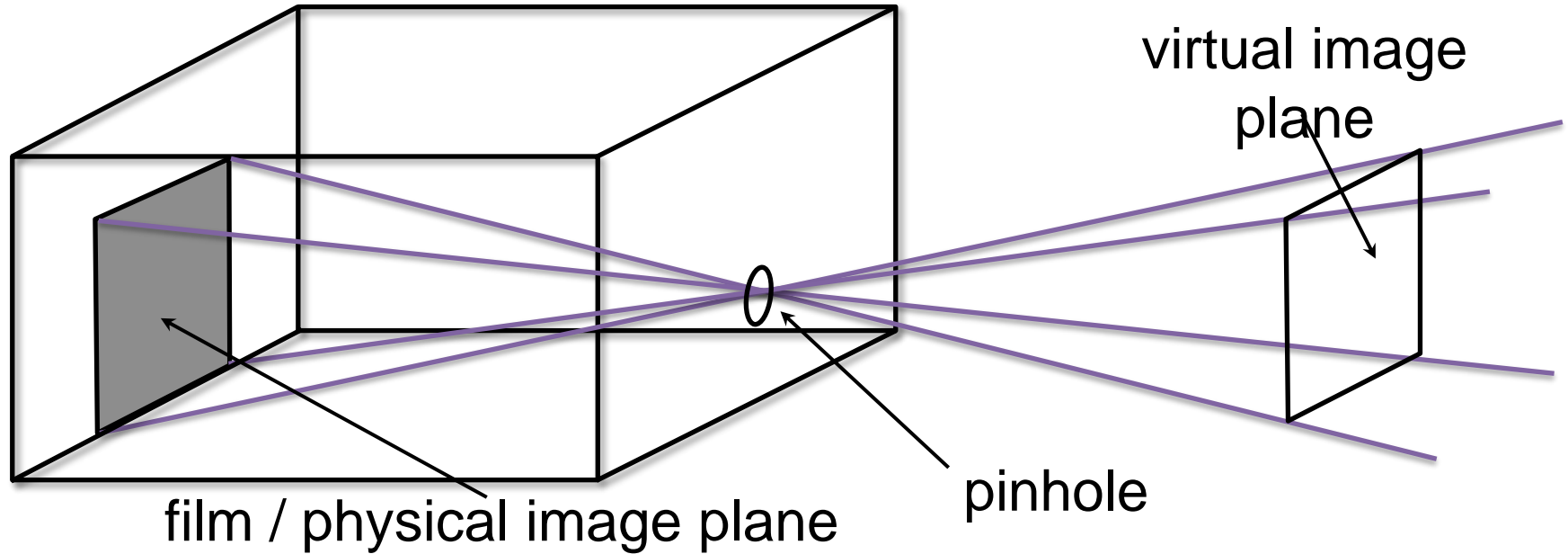
- Basic pipeline





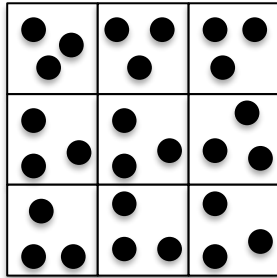
# Ray Generation

- Pinhole camera



# Ray Generation

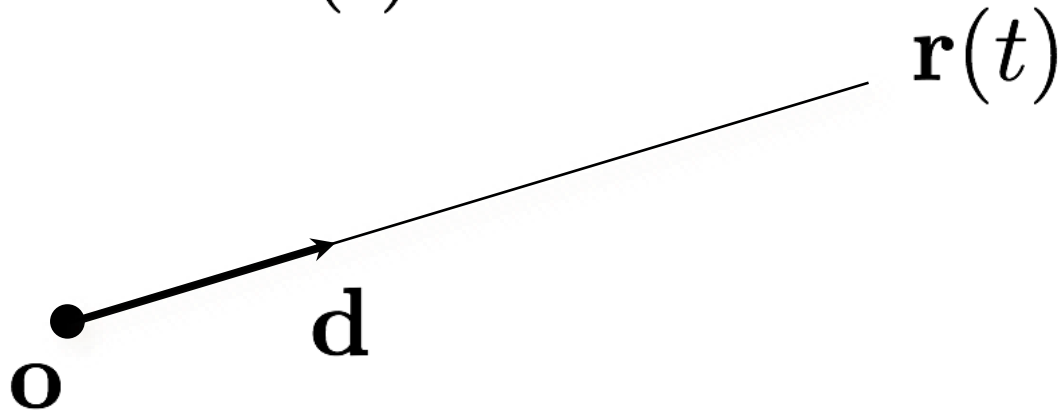
- Extension – Anti-aliasing
  - Multiple rays per pixel - supersampling



# Ray-Surface Intersections

- Ray equation

$$\mathbf{r}(t) = \mathbf{o} + t\mathbf{d}$$



# Ray-Surface Intersections

- Sphere

- Equation

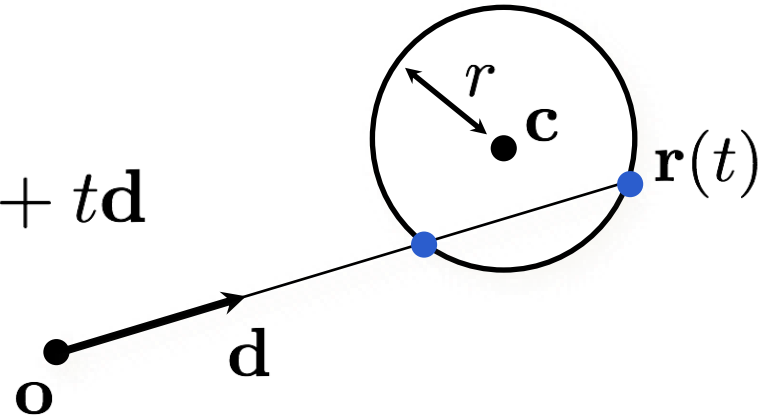
$$\|\mathbf{x} - \mathbf{c}\|^2 - r^2 = 0$$

point of interest      center      radius

- Insert ray equation  $\mathbf{r}(t) = \mathbf{o} + t\mathbf{d}$

- Solve for t

$$\|\mathbf{o} + t\mathbf{d} - \mathbf{c}\|^2 - r^2 = 0$$



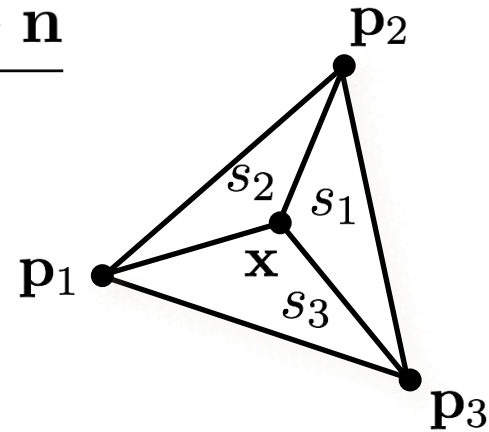
# Ray-Surface Intersections

- Triangle

- Barycentric coordinates  $\mathbf{x} = s_1\mathbf{p}_1 + s_2\mathbf{p}_2 + s_3\mathbf{p}_3$
- Intersect with triangle's plane

$$(\mathbf{o} + t\mathbf{d} - \mathbf{p}_1) \cdot \mathbf{n} = 0 \quad t = -\frac{(\mathbf{o} - \mathbf{p}_1) \cdot \mathbf{n}}{\mathbf{d} \cdot \mathbf{n}}$$

- where  $\mathbf{n} = (\mathbf{p}_2 - \mathbf{p}_1) \times (\mathbf{p}_3 - \mathbf{p}_1)$
- Compute  $s_i$
- Test  $s_1 + s_2 + s_3 = 1 \quad 0 \leq s_i \leq 1$

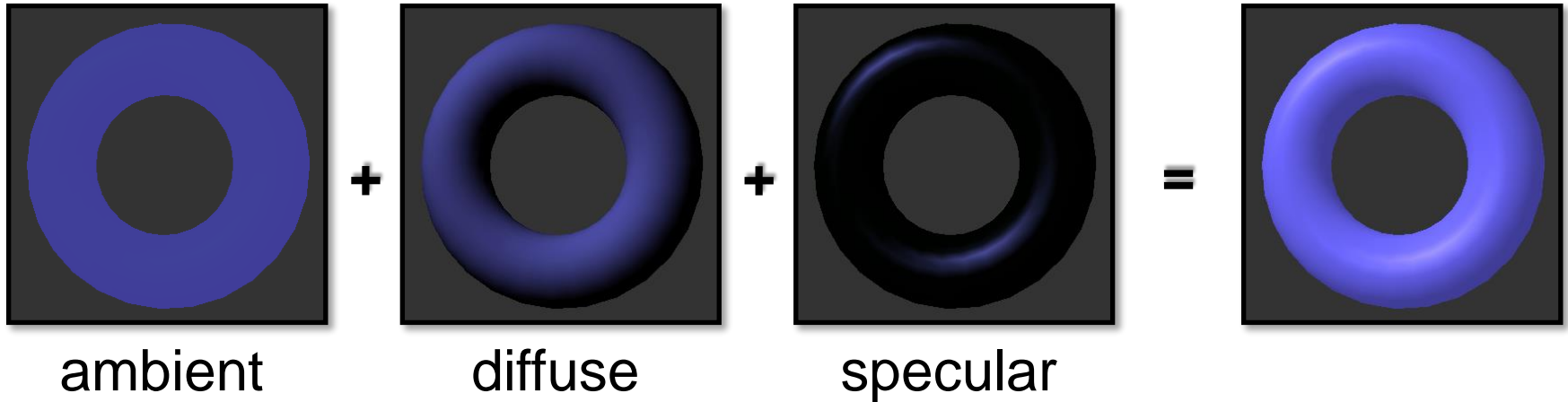


# Shading

- Physically exact shading too costly
- Simplifying assumptions
  - **Surface reflectance**: diffuse, specular, ambient, transparency terms
  - **Shadows**: shadow rays to determine if a hit point is in shadow or not

# Shading

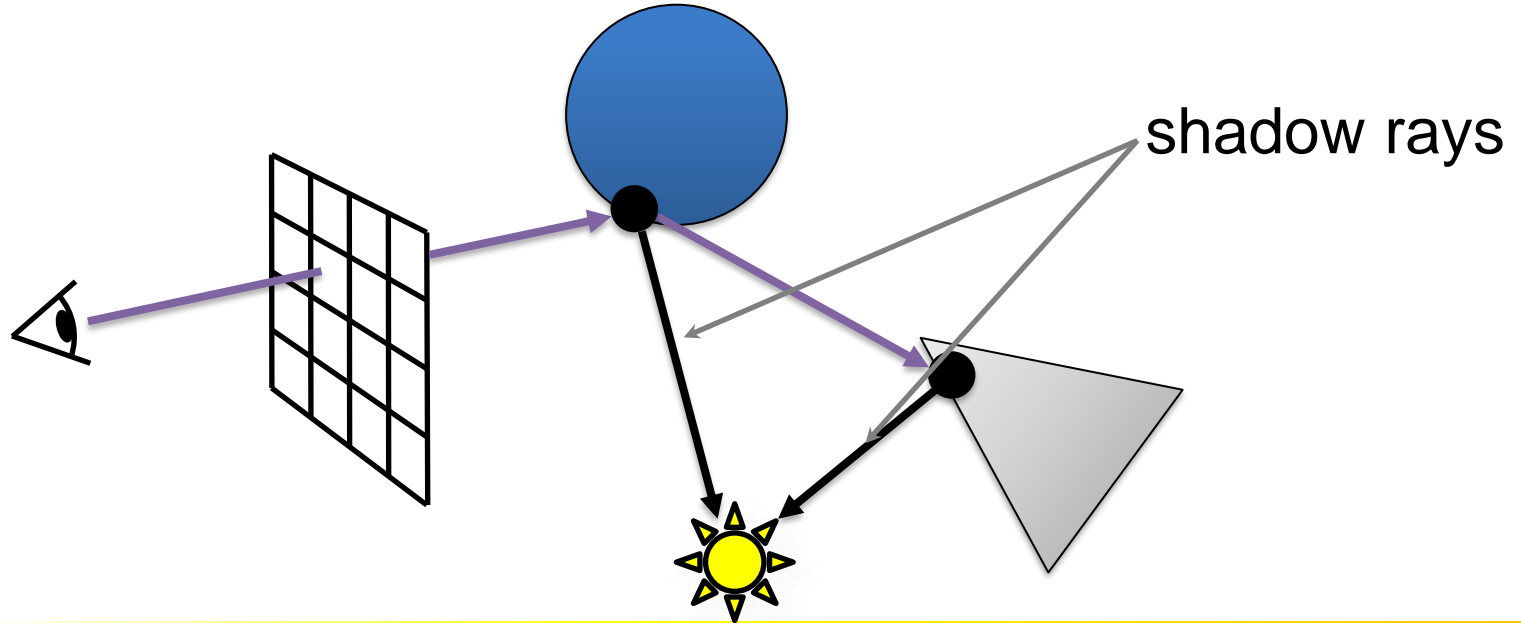
- Simplifying assumptions – surface reflectance



(see lighting and shading slides)

# Shading

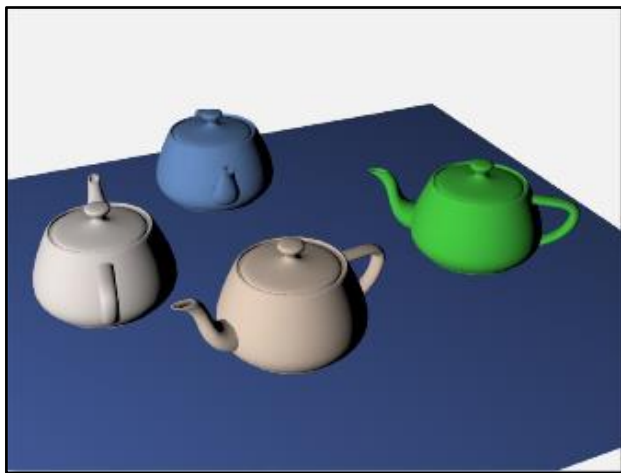
- Simplifying assumptions – shadows



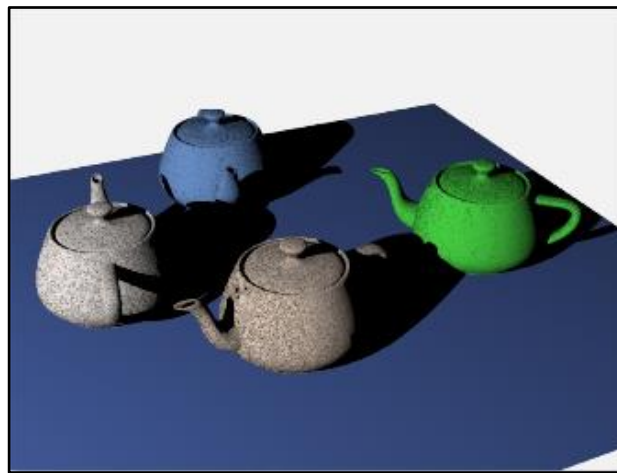


# Shading

- Simplifying assumptions – shadows



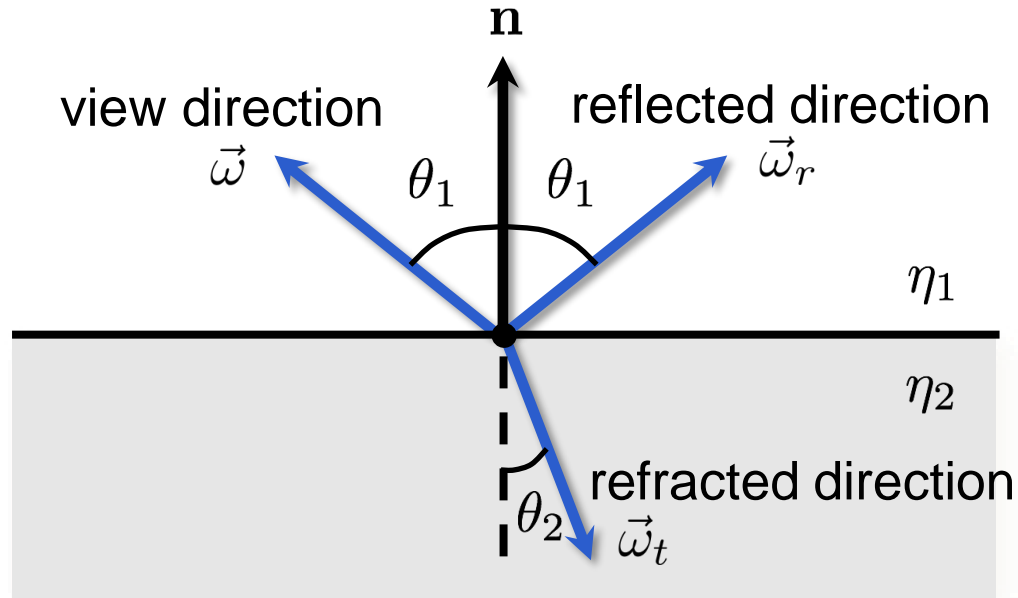
Diffuse shading



With shadows

# Shading

- Extensions – Refraction



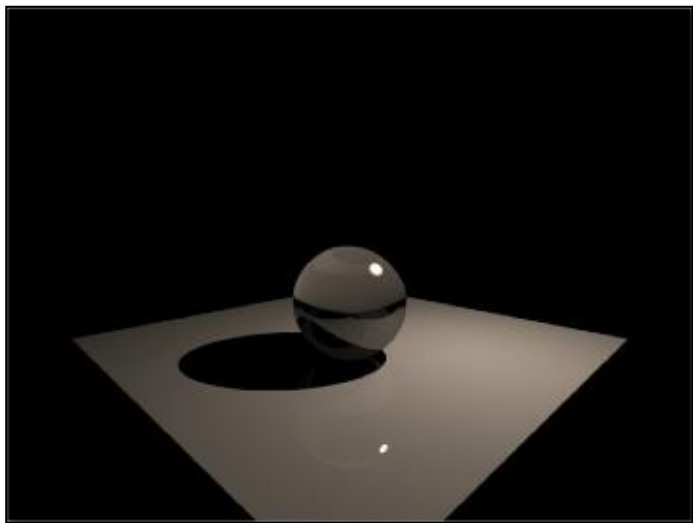
# Shading

- Extensions – Refraction

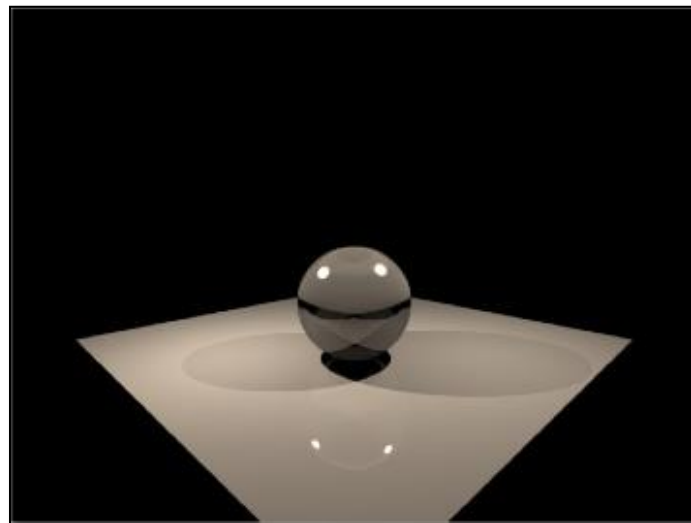


# Shading

- Extensions – Multiple lights



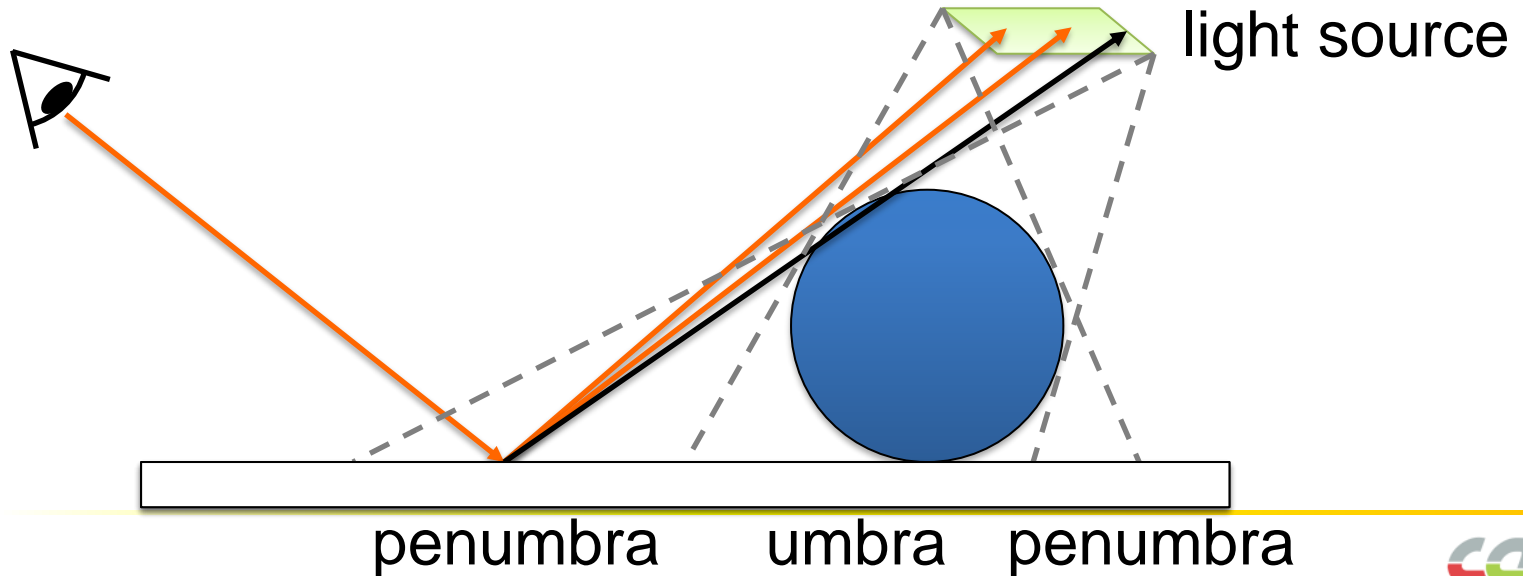
One light



Two lights

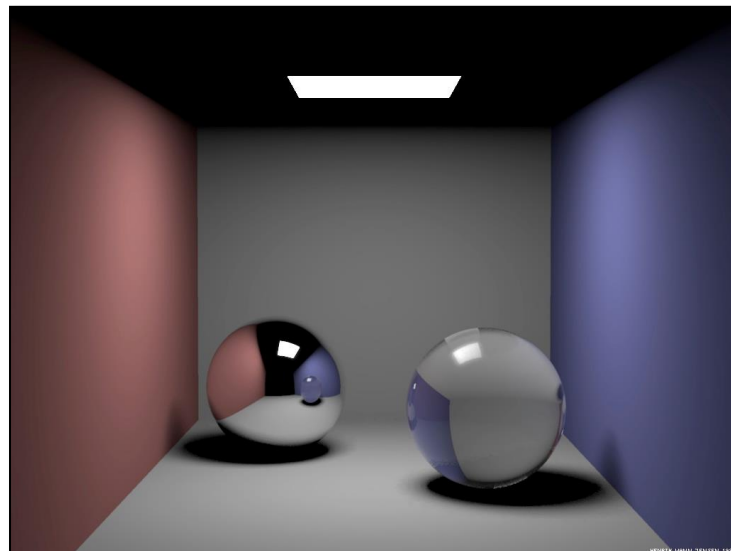
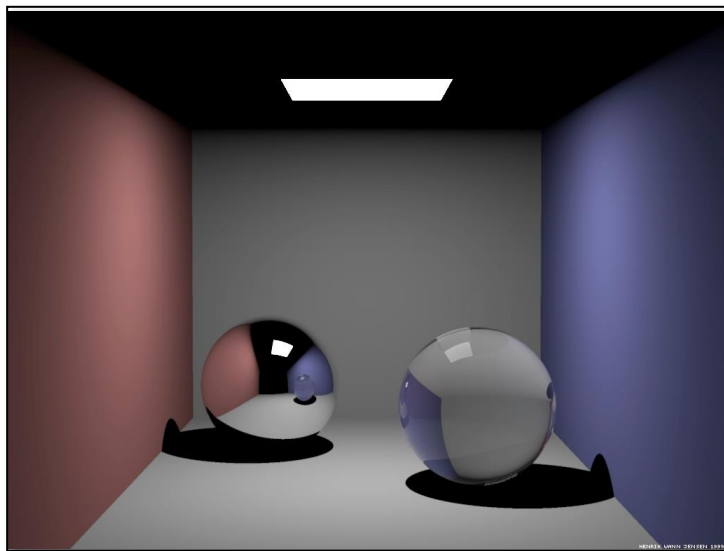
# Shading

- Extensions – Area lights for soft shadows
  - Multiple shadow rays to sample area light source



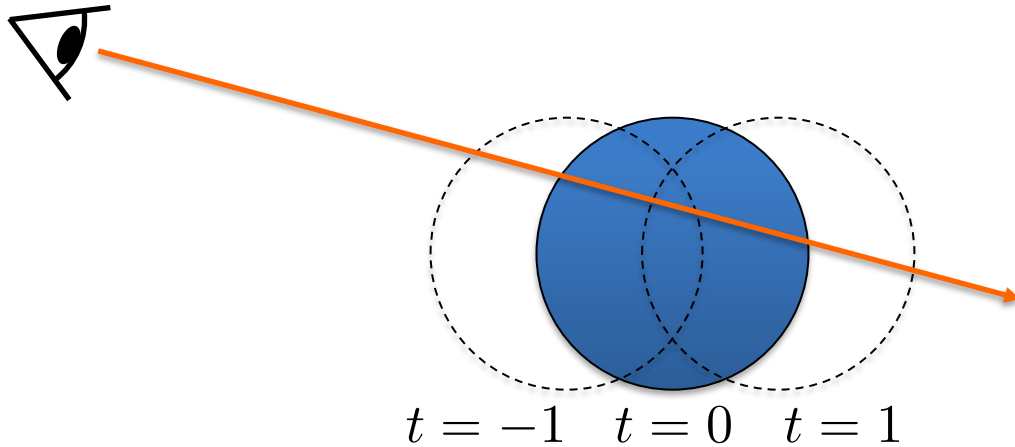
# Shading

- Extensions – Area lights for soft shadows



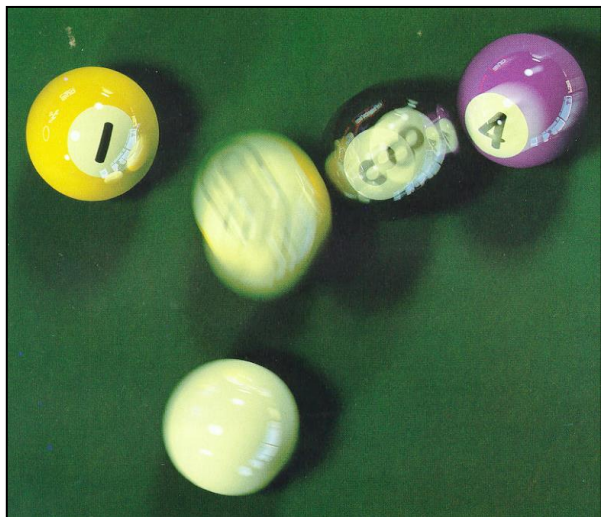
# Shading

- Extensions – Motion blur
  - Sample objects and intersect in time



# Shading

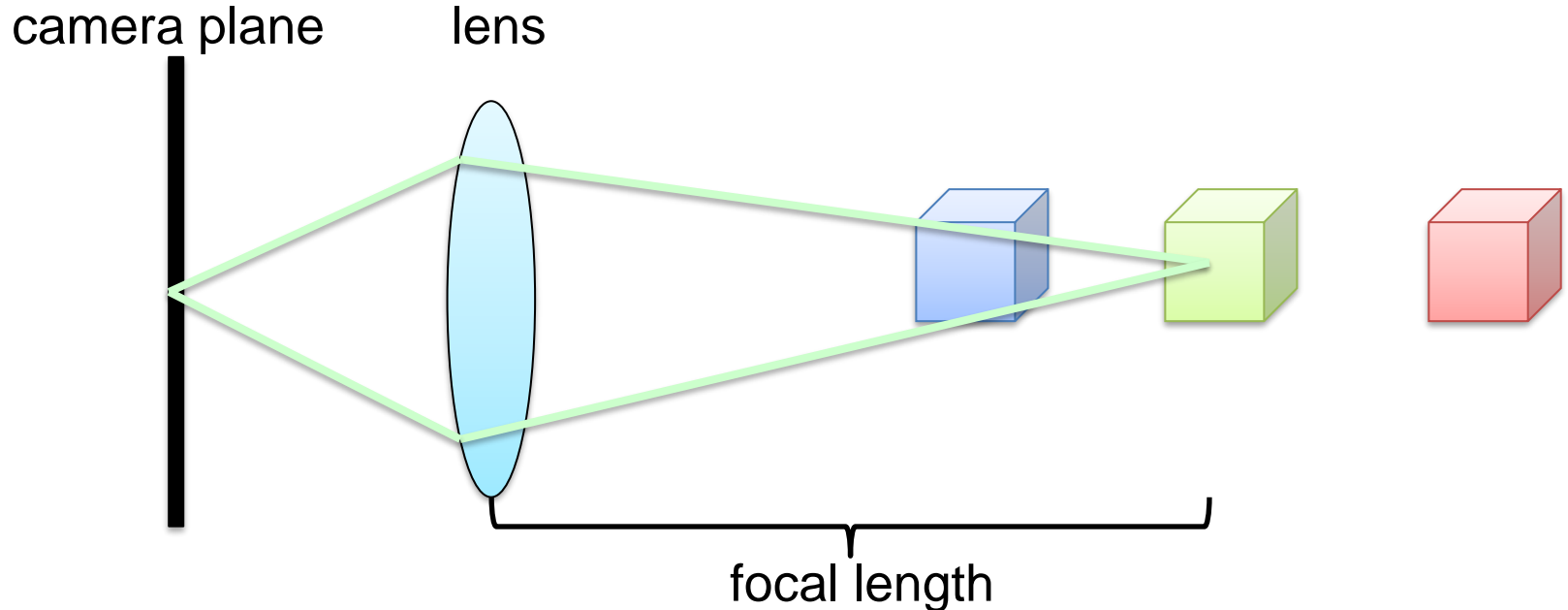
- Extensions – Motion blur





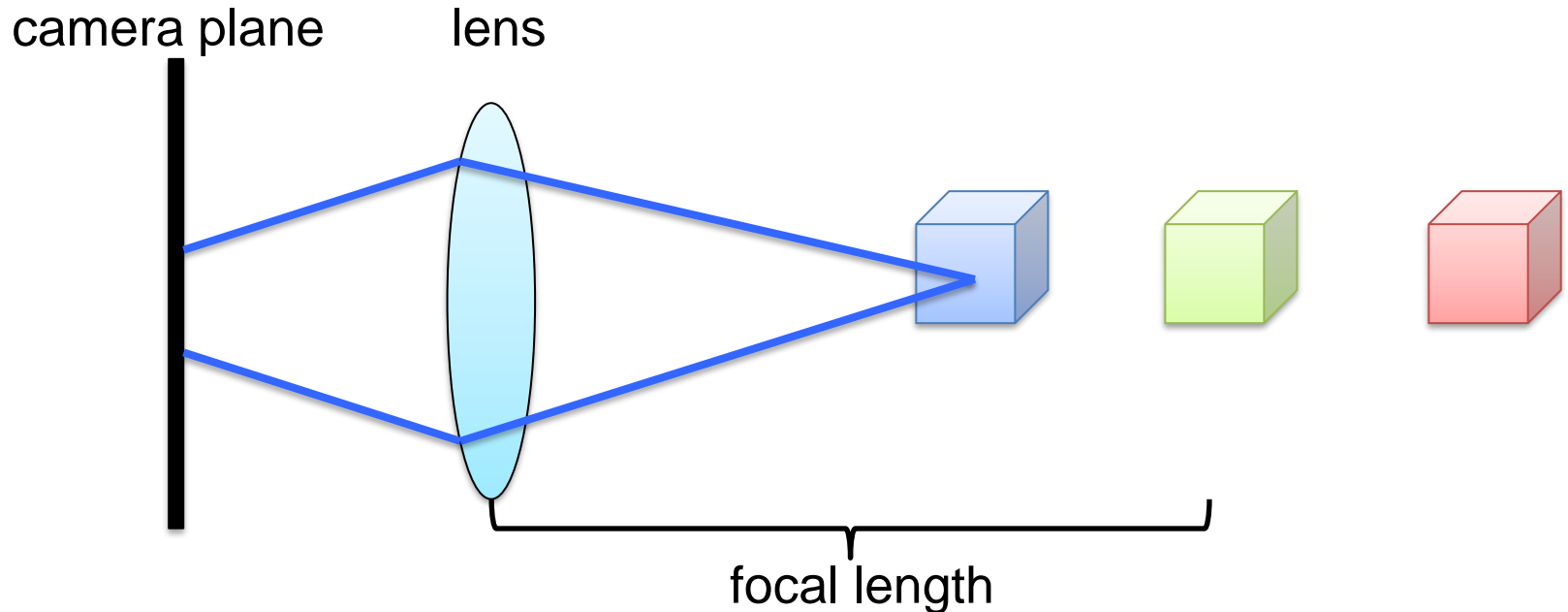
# Shading

- Extensions – Depth of field



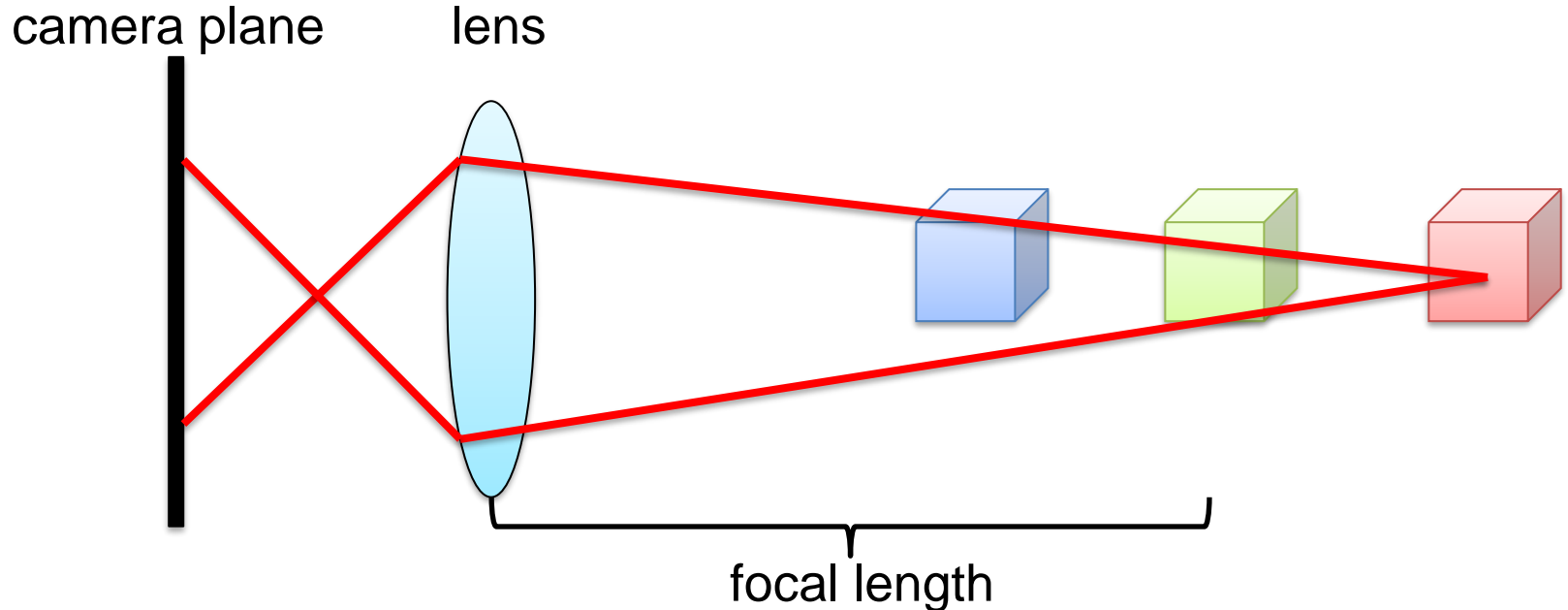
# Shading

- Extensions – Depth of field



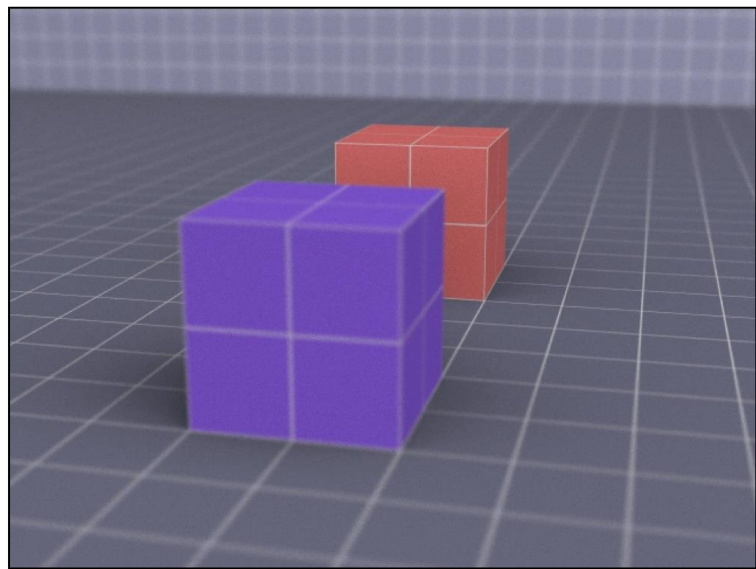
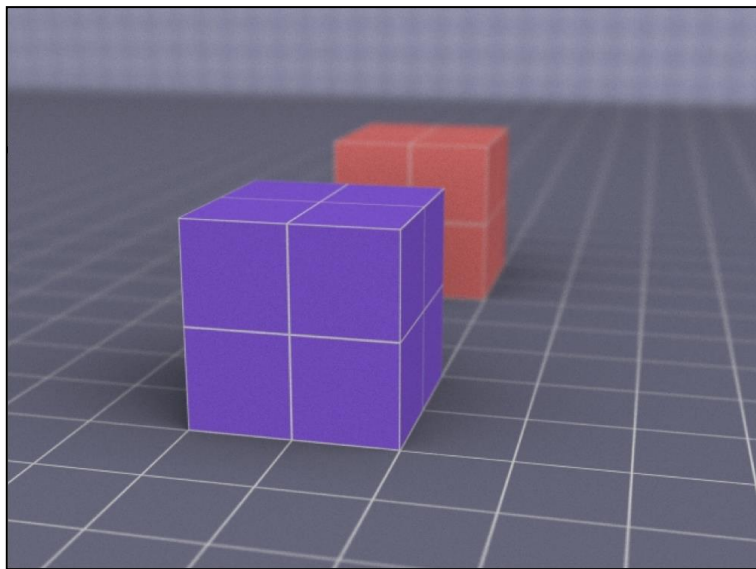
# Shading

- Extensions – Depth of field



# Shading

- Extensions – Depth of field



# Acceleration

- Complex scenes
  - Cost =  $O(\#rays \times \#objects)$
  - 50K trees each with 1M polygons = 50B polygons  
→ **594 years!**



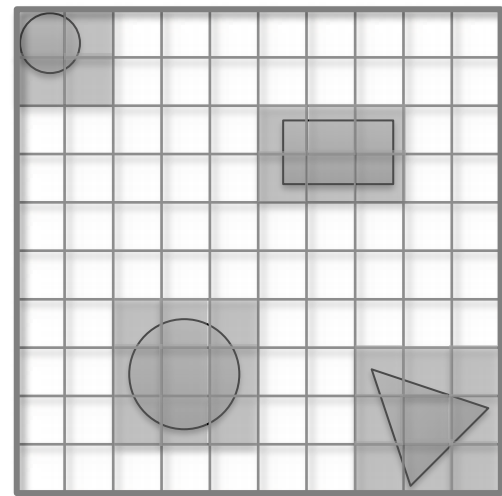
# Acceleration

- Solution: fewer intersections
  - Uniform grids
  - Space partitioning trees
- 11 minutes – 300,000,000x speedup



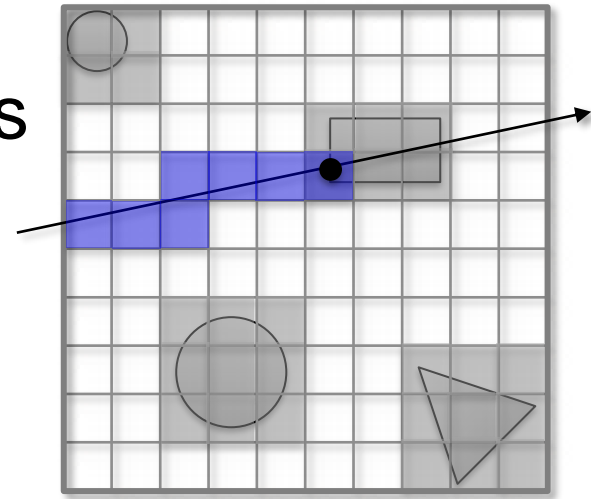
# Acceleration

- Uniform grids – Preprocessing
  - Compute bounding box
  - Set grid resolution
  - Rasterize objects
  - Store references to objects



# Acceleration

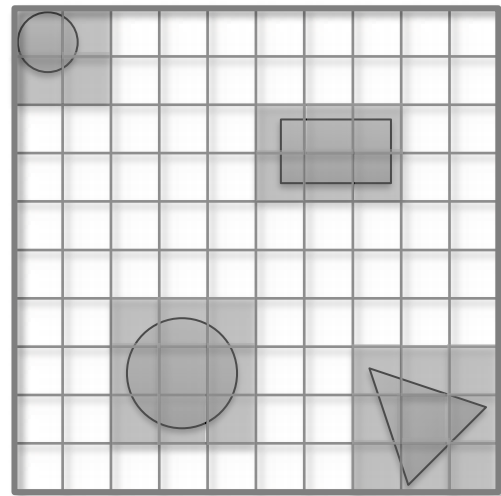
- Uniform grids – Traversal
  - Incrementally rasterize ray
  - Stop when intersection happens





# Acceleration

- Uniform grids
- Advantages
  - Fast to build
  - Easy to code
- Disadvantages
  - Non-adaptive to scene geometry

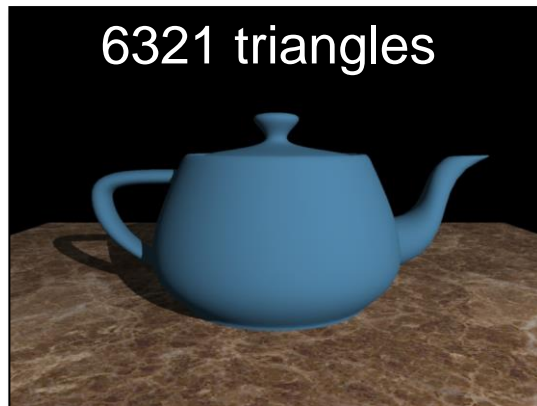


# Acceleration

- Uniform grids

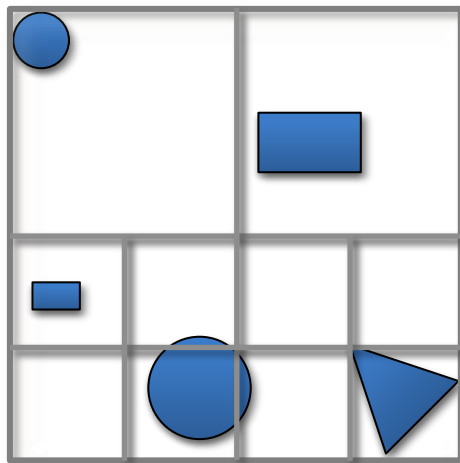
Brute force: 6321 intersection tests per ray

Uniform grid: 44.86 intersection tests per ray

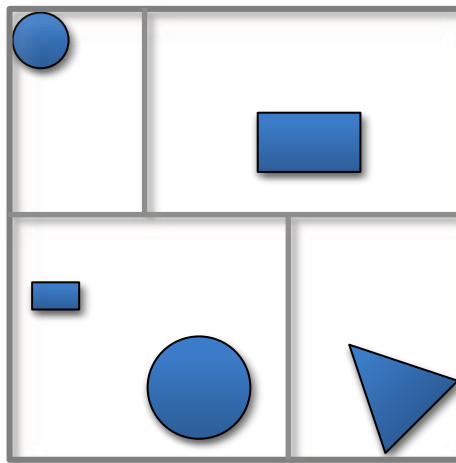


# Acceleration

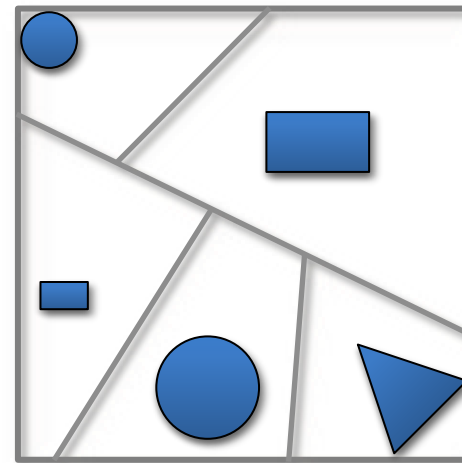
- Space partitioning trees



octree



kd-tree



bsp-tree